

# NOTES ON CHAPTER 3 OF BEAVER (2001)

## AND A GLIMPSE OF CHAPTER 4

04.03.08

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## 1 The Big Picture

- Why do *we* care about presupposition?
  - Presumably because it's connected to important issues in the science of language, communication and meaning
- Beaver (2001) is dedicated to theories of **presupposition projection**:
  - How are the presuppositions of an *utterance* of a sentence  $S$  calculated from the presuppositions of  $S$ 's constituents?
- If you're in a divisive mood, you might think there are two very different kinds of answers to this question:

**Pragmatic Answers** The presuppositions of an utterance of  $S$  are determined both by what speakers tend to take for granted when they utter sentences with  $S$ 's constituents as well as certain independently motivated generalization about communication. (Stalnaker 2002: 703, among others)

**Semantic Answers** The presuppositions of  $S$  are compositionally determined from  $S$  constituents just as  $S$ 's meaning is. The presuppositions may be themselves part of the meaning (hence the compositional isomorphism) or computed in a 'separate dimension' parallel to the computation of the non-presuppositional component.

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## 2 Filtration & Cancellation Theories of Presupposition

- Karttunen's (1973) analysis is an example of **Local Filtering** (Bottom-Up)
  - For each subsentence of  $S$  consisting of an operator embedding further subsentences as arguments,  $S$  not only carries its own potential presuppositions, but also inherits a subset of the potential presuppositions of the arguments
- On the other hand, Gazdar (1979); Mercer (1987, 1992) and van der Sandt's (1988) analyses are examples of **Global Cancellation** (Top-Down)
  - Pragmatic principles determine a function from tuples consisting of the context, the set of potential presuppositions, the assertive content of the sentence, and (except in van der Sandt's theory) a set of Gricean implicatures of the sentence, to that subset of the potential presuppositions which is projected

### 2.1 Filtration: Karttunen 1973

- Terminology:
    - Plugs** predicates which block off all of the presuppositions of the complement sentence, e.g. *say, mention, tell, ask*
    - Holes** predicates or connectives which let all the presuppositions of the complement sentence become presuppositions of the matrix sentence, e.g. *know, regret, understand, be possible, not, realize*
    - Filters** predicates or connectives which, under certain conditions, cancel some of the presuppositions of the arguments, e.g. *if then, either or, and*
  - The Theory:
    - Definition 7** (Beaver 2001: 56)
      - $\pi(S)$  is the set of **potential presuppositions** of  $S$
      - $F$  is a possibly null set of **contextually assumed facts** (sentences)
      - $P_F(S)$  maps  $S$  to the set of **sentences it presupposes** relative to  $F$
1.  $P_F(S) = \pi(S)$  if  $S$  is simple
  2.  $P_F(S) = P_F(S_1) \cup \pi(S)$  if  $S$  contains a hole predicate embedding  $S_1$
  3.  $P_F(S) = \pi(S)$  if  $S$  contains a plug predicate embedding any sentence
  4.  $P_F(S) = P_F(S_1) \cup \{p \in P_F(S_2) \mid (F \cup \{S_1\}) \neq p\}$  if  $S = \text{'If } S_1 \text{ then } S_2\text{'}$  or  $S = \text{'}S_1 \text{ and } S_2\text{'}$
  5.  $P_F(S) = P_F(S_1) \cup \{p \in P_F(S_2) \mid (F \cup \{\neg S_1\}) \neq p\}$  if  $S = \text{'Either } S_1 \text{ or } S_2\text{'}$

- An example:

(1) If  $[\text{A} \text{Kay's dog is dead}]$  then  $[\text{B} \text{Dee doesn't realize Kay's dog is dead}]$

- Let  $C = \text{'Dee does realize } [\text{A} \text{Kay's dog is dead}] \text{'}$  and  $F = \emptyset$
- Observation (given by the grammar):

$$\pi(\text{A}) = \{\text{Kay has a dog}\} \quad (2)$$

$$\pi(\text{B}) = \{\text{Kay has a dog, Kay's dog is dead} = \text{A}\} \quad (3)$$

$$\pi(\text{C}) = \{\text{Kay has a dog, Kay's dog is dead} = \text{A}\} \quad (4)$$

- Let's first find  $P_F(\text{B})$ :

$$\begin{aligned} P_F(\text{B}) &= P_F(\text{C}) \cup \pi(\text{B}) && \text{(by D7.2)} \\ &= (P_F(\text{A}) \cup \pi(\text{C})) \cup \pi(\text{B}) && \text{(by D7.2)} \\ &= (\pi(\text{A}) \cup \pi(\text{C})) \cup \pi(\text{B}) && \text{(by D7.1)} \\ &= \{\text{Kay has a dog, Kay's dog is dead}\} && \text{(by (2)-(4))} \\ &= \pi(\text{B}) && \text{(by 3)} \end{aligned} \quad (5)$$

Now we find  $P_F((1))$ :

$$\begin{aligned} P_F((1)) &= P_F(\text{A}) \cup \{p \in P_F(\text{B}) \mid (F \cup \{\text{A}\}) \not\models p\} && \text{(by D7.4)} \\ &= P_F(\text{A}) \cup \{p \in \pi(\text{B}) \mid (\emptyset \cup \{\text{A}\}) \not\models p\} && \text{(by (5), } F = \emptyset\text{)} \\ &= P_F(\text{A}) \cup \emptyset && \text{(by (3), } \text{A} \models \text{Kay has a dog}\text{)} \quad (6) \\ &= \pi(\text{A}) \cup \emptyset && \text{(by D7.1)} \\ &= \{\text{Kay has a dog}\} \quad \checkmark && \text{(by (2))} \quad (7) \end{aligned}$$

- So (1) is predicted to presuppose *Kay has a dog* in  $F$
- Does  $\text{A}$  entail *Kay has a dog* or merely presuppose it?
  - ▷ It seems like we have to take a stand on this in step (6)
  - ▷ In this case, it didn't matter, but it could've
  - ▷ Should this whole system be stated on a semantic level rather than on a syntactic one?

- Another example:

(8) Either  $[\text{A} \text{Geraldine is not a Mormon}]$  or  $[\text{B} \text{she has given up wearing holy underwear}]$

- The data: (8) does not presuppose that Geraldine is a Mormon
- Yet, if  $F = \emptyset$  Karttunen predicts that (8) presupposes that *Geraldine wore holy underwear at some past time*
  - ▷ By D7.5, each presuppositions of  $\text{B}$  project to (8) unless  $\neg\text{A}$  or  $F$  entail it
  - ▷  $\pi(\text{B}) = \{\text{Geraldine wore holy underwear at some past time}\}$
  - ▷  $\neg\text{A} = \text{Geraldine is a Mormon}$  does not entail *Geraldine wore holy underwear at some past time*
  - ▷ So, the latter projects when  $F = \emptyset$

- ▷ However, if you stipulate

$F = \{\text{All Mormons have worn holy underwear at some past time}\}$ , then the entailment goes through and the troubling presupposition is blocked

- ▷ This is Karttunen's way of getting the correct prediction for (8)

- Yet another example:

(9)  $[\text{A} \text{Jay doesn't regret writing a boring dissertation}]$ , because he didn't write a dissertation

- According to Karttunen's analysis:

▷  $P_F(\text{A}) = \pi(\text{A}) = \{\text{Jay wrote a boring dissertation, ...}\}$ , since *not* is a hole and *Jay does regret writing a boring dissertation* seems to presuppose *Jay wrote a boring dissertation*

- But this alleged presupposition is denied in the *because*-clause of (9), which you shouldn't be able to do if it's genuinely a precondition for  $\text{A}$ 's truth
- (9) is an example of **presupposition denial** (Levinson 1983: 194-195)
- As Beaver (2001: 70) notes, Karttunen's filtration theory does not make the correct prediction on presupposition denial cases without stipulating that there are two *not*'s, one that's a plug and one that's a hole
  - ▷ Fine if you can motivate it, but there's no known independent evidence for it

- Questions:

- Where does  $F$  come from?
- What kinds of facts do the clauses in Definition 7 represent?

- Cancellation theories offer improvements on both of these fronts

## 2.2 Cancellation Theories

### 2.2.1 Gazdar (1979)

- Gazdar (1979) also considers it crucial to calculate presuppositions in context
  - For Gazdar, a context  $C$  seems to be an agent's representation of the conversational participants' knowledge
- However, Gazdar aims to give a quasi-Gricean analysis of presupposition
  - He aims to reduce presupposition projection to more general processes of reasoning
    - ▷ More specifically, the processes of reasoning involved in maintaining a representation of what the speakers in a conversation have committed themselves to knowing
  - Gazdar uses Hintikka's (1962) logic of knowledge and belief (LKB) to represent these knowledge commitments
  - This approach is Gricean in that it aims to ground presupposition projection in general processes of reasoning about our interlocutor's mental states
  - What's not clearly Gricean about the picture is that these processes of reasoning may

not be justified by their contribution to successful co-operation, but rather by standards of rationality that apply to agents in isolation

- Let's talk about this after we see the theory, but I want everyone to keep it in mind as we work through it
- For Gazdar the presuppositions of an utterance of **S** in context  $C$  are calculated as follows:
  - **S** is translated into LKB
    - ▷ Let  $\alpha$  be this translation
  - $K(\alpha)$  is added to  $C$  ( $C$  is a set of LKB wffs); call the result  $C'$ 
    - ▷  $K(\alpha)$  means the speaker knows that  $\alpha$
    - ▷  $K$  satisfies necessitation:  $K(\phi) \models \phi$
  - $C'$  is then updated with every **potential implicature** of **S** that does not introduce inconsistency; call the result  $C''$ 
    - ▷  $\iota(\mathbf{S}) :=$  The set of each potential implicature of **S** translated into LKB
  - Last,  $C''$  is updated with every **potential presupposition** of **S** that does not introduce inconsistency
    - ▷  $\pi(\mathbf{S}) :=$  The set of potential presuppositions of **S** translated into LKB
    - ▷ Presuppositions are represented epistemically, so that if **S** 'presupposes'  $\phi$  then  $K(\phi) \in \pi(\mathbf{S})$ 
      - ▶ Similar to Stalnaker's (2002) idea that presupposing is a propositional attitude, except Stalnaker goes for a more plausible logic, the logic of *common belief* (Fagin *et al.* 1995), but does the *Stalnaker shuffle* when it comes to developing a formally explicit and concrete proposal about how projection might work
- The effect of updating with implicatures before presuppositions is that if a presupposition conflicts with an implicature, the presupposition is cancelled
- To make this calculation precise, Gazdar gives a definition of what it is to add all of the presuppositions or implicatures that do not **introduce inconsistency**
  - This is his notion of **satisfiable incrementation**
- For any sets  $X, Y, Z$  of LKB wffs:

**Definition 8** (Consistency, Satisfiable Incrementation)

$$\begin{aligned}
 cons(X) &\iff X \not\models \perp \\
 X \cup Y &= X \cup \{y \in Y \mid \forall Z \subseteq (X \cup Y) : cons(Z) \implies cons(Z \cup \{y\})\} \\
 &= X \cup \text{every } y \in Y \text{ that preserves consistency when added to any} \\
 &\quad \text{consistent subset of } X \cup Y
 \end{aligned}$$

- Given this, the calculation of **S**'s presuppositions in  $C$  can be defined as follows, where **S**'s LKB translation is  $\alpha$ :

**Definition 9** (Gazdarian Update)

$$\begin{array}{c}
 C' = ((C \cup \{K(\alpha)\}) \cup \iota(\mathbf{S})) \cup \pi(\mathbf{S}) \\
 \hline
 +\text{Assertion} \\
 \hline
 +\text{Implicature} \\
 \hline
 +\text{Presupposition}
 \end{array}$$

- An example:
  - (10) If Mary is sleeping then Fred is annoyed that she is sleeping
  - Let  $C = \emptyset$ ,  $\alpha = \text{Sleeping}(m) \rightarrow \text{Annoyed}(f, \text{Sleeping}(m))$

$$\iota((10)) = \left\{ \begin{array}{ll} \neg K(\text{Sleeping}(m)), & \neg K(\neg \text{Sleeping}(m)), \\ \neg K(\text{Annoyed}(f, \text{Sleeping}(m))), & \neg K(\neg \text{Annoyed}(f, \text{Sleeping}(m))) \end{array} \right\} \quad (11)$$

$$\pi((10)) = \{K(\text{Sleeping}(m))\} \quad (12)$$

- Calculate the assertion and implicatures first:

$$\begin{aligned}
 (C \cup \{K(\alpha)\}) \cup \iota((10)) &= \{K(\alpha)\} \cup \iota((10)) && (C = \emptyset) \\
 &= \text{Every } p \in \{K(\alpha)\} \cup \iota((10)) \text{ consistent} \\
 &\quad \text{with every consistent subset of } \{K(\alpha)\} \cup \iota((10)) && \text{(by D8)} \\
 &= \{K(\alpha)\} \cup \iota((10)) && (13) \\
 &=: I && \text{(intro. notation)} \\
 & && (14)
 \end{aligned}$$

- We get (13) since every subset of  $\{K(\alpha)\} \cup \iota((10))$  is consistent and every  $p \in \iota((10))$  is consistent with every subset of  $\{K(\alpha)\} \cup \iota((10))$ 
  - ▷ It's tedious to show this in full detail, but is fairly clear from looking at (10)
    - ▶ No two implicatures are inconsistent, no implicature is inconsistent with  $K(\alpha)$ , and no implicature or implicatures entail something inconsistent when taken with  $K(\alpha)$ , so clearly every subset of  $\{K(\alpha)\} \cup \iota((10))$  is consistent and every element of such a subset is consistent with every other subset

- Now calculate the presuppositions:

$$\begin{aligned} ((C \cup \{K(\alpha)\}) \cup !\iota((10))) \cup !\pi((10)) &= I \cup !\pi((10)) && \text{(by (13), (14))} \\ &= I \cup !\{K(\text{Sleeping}(m))\} && \text{(by (12))} \\ &= I && (15) \end{aligned}$$

- The move to (15) is justified by the following:
  - ▷ There's only one  $p \in \{K(\text{Sleeping}(m))\}$ :  $K(\text{Sleeping}(m))$
  - ▷ But  $K(\text{Sleeping}(m))$  is not consistent with every consistent subset of  $I \cup \{K(\text{Sleeping}(m))\}$
  - ▷ Since  $\neg K(\text{Sleeping}(m)) \in I$ , just consider  $\{\neg K(\text{Sleeping}(m))\}$
  - ▷ So by D8,  $I \cup \{K(\text{Sleeping}(m))\} = I \cup \emptyset = I$
- Intuitively, the one potential presupposition of (10),  $K(\text{Sleeping}(m))$ , conflicts with one of its genuine implicatures:  $\neg K(\text{Sleeping}(m))$ 
  - ▷ But, implicatures get priority, so the presupposition gets cancelled
- Comments:
  - Unlike  $F$  in Karttunen's theory, it's clear where  $C$  comes from; it's maintained dynamically as the discourse unfolds
  - Projection facts are not primitive, as they are in Karttunen's theory
  - Projection patterns are taken to arise from a general process of rational context maintenance
  - Unlike Karttunen's theory, Gazdar's theory can correctly predict presupposition denial cases like (9) (homework [hint: the problematic presupposition gets cancelled by an implicature])
- But, there are some significant challenges for Gazdar's theory, both theoretical and empirical
  - Unlike, Karttunen's theory, Gazdar's theory makes the incorrect prediction for:
    - (16) If none of Mary's friends come to the party, she'll be surprised that her best friends aren't there
      - ▷ The consequent introduces the potential presupposition that the speaker knows that Mary's best friends aren't at the party
        - ▶ The relevant clausal implicature introduced by the antecedent is that the speaker does not know whether or not **none** of Mary's friends are coming to the party
        - ▶ But this isn't strong enough to cancel the presupposition, since it's consistent with it being known that just Mary's **best** friends aren't coming
      - ▷ So Gazdar's theory predicts that (16) presupposes that Mary's best friends aren't coming to her party, which is clearly incorrect
      - ▷ On the other hand, Karttunen gets it right, since (by D7.4) the only presuppositions that project from the consequent are those not entailed by the antecedent
        - ▶ *None of Mary's friends come to the party* entails *Mary's best friends don't*

*come to the party*

- ▶ So, the latter does not project
- Questions:
  - Why is it rational to update contexts according to Definition 8?
    - ▷ Satisfiable incrementation involves consistency preservation, which is rational regardless of whether or not you are taking part in a collaborative exchange
    - ▷ But, satisfiable incrementation also involves adding as much information as possible
      - ▶ Why is this rational?
      - ▷ More interestingly, why are implicatures added before presuppositions?
        - ▶ Without this feature of the theory, nothing is achieved
    - Where does the set of potential implicatures,  $\iota(S)$ , come from?
      - ▷ One relevant detail:  $\iota(S)$  is taken to represent something like the hearer's hypotheses about the implicatures of  $S$
      - ▷ How stable are these hypotheses and what resources are used to generate them? It doesn't seem to be plausible that our knowledge of grammar provides it, and that's the only *we can take them as given* strategy that seems coherent
      - ▷ Whatever the answer is, it seems like there has to be a lot more to Gazdar's theory than we've been given here

### 2.2.2 Mercer (1987; 1992)

[Mercer \(1987, 1992\)](#)

### 2.2.3 van der Sandt (1982; 1988)

[van der Sandt \(1982, 1988\)](#)

## 2.3 Combination Theories

- Given the complementarity of Karttunen's theory and Gazdar's theory, one might try to combine them
- The least intelligent way to achieve this is by running both theories on a sentence and taking the intersection of their predicted presuppositions, since each theory alone has been shown to **overgenerate**
- Maybe some hybrid can be formed?
- Maybe, but it would still face major difficulties based on the following examples

## 2.4 Quantification & Conditionals

- Consider:
  - (17) Exactly one woman realized that if her watch was slightly wrong, she'd be in danger of shooting the wrong man
    - What (17) presupposition is triggered by *her watch*?
      - ▷ Intuitively, *the woman having the realization has a watch*
      - ▷ But what do Karttunen and Gazdar predict?
      - ▷  $\text{watch}(x)$ , where  $x$  has the effect of universal quantification?
        - ▶ No, the relevant presupposition should be restricted to some salient set of women
      - ▷  $\lambda x.\text{watch}(x)$ 
        - ▶ No, because that would not project out of the antecedent (on either theory)
        - ▶ It would predict that the assertion of (17) amounts to *exactly one woman came to believe that if she owned a watch and that watch was slightly wrong then she would be in danger of shooting some wrong man*
        - ▶ But this misses the fact that (17) seems to entail/presuppose that the woman mentioned actually does own a watch!
- Also consider:
  - (18) If LBJ appoints J. Edgar Hoover to the cabinet, he will regret having appointed a homosexual

## 3 Dynamic Theories of Presupposition

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